

Section 6.6 Transformations

$$f(x) = a \sin(x-c) + d$$

$a \rightarrow$ vertical stretch/compression

$a > 0$ vertical stretch

$0 < a < 1$ vertical compression

$a < 0$ - reflection

$c \Rightarrow$ horizontal translation

$d \Rightarrow$ vertical translation

Both a & d effect the range (max/min and equation of the axis of symmetry)

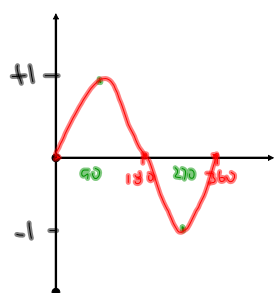
$$\text{range } R = \{y \in \mathbb{R} \mid \min \leq y \leq \max\}$$

Eqn of the axis $y = d$

$$\begin{aligned} \max &= d + a \\ \min &= d - a \end{aligned} \quad \left. \vphantom{\begin{aligned} \max &= d + a \\ \min &= d - a \end{aligned}} \right\} \text{ if } a \text{ is greater than zero}$$

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Base Function $f(x) = \sin x$ 

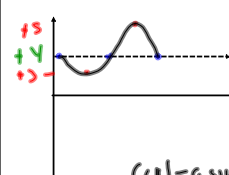
0	0
90	+1
180	0
270	-1
360	0

$$f(x) = a \sin(x-c) + d$$

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i) The function $f(x) = \sin x$ is reflected across the x axis and translated up 4 units. State the new equation.

$$y = -\sin x + 4$$



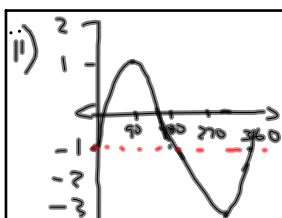
$$f(x) = a \sin(x-c) + d$$

$$f(x) = -\sin x + 4$$

$$\begin{aligned} d &= +4 \\ a &= -1 \end{aligned}$$

0	4
90	3
180	4
270	3
360	4

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$$y = a \sin(x-c) + d$$

$$d = \frac{\max + \min}{2}$$

$$= \frac{1 + -3}{2}$$

$$= -1$$

$$y = 2 \sin x - 1$$

$$\begin{aligned} a &= 2 \\ d &= -1 \end{aligned}$$

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Graph

$$f(x) = -2 \sin(x+30) + 5$$

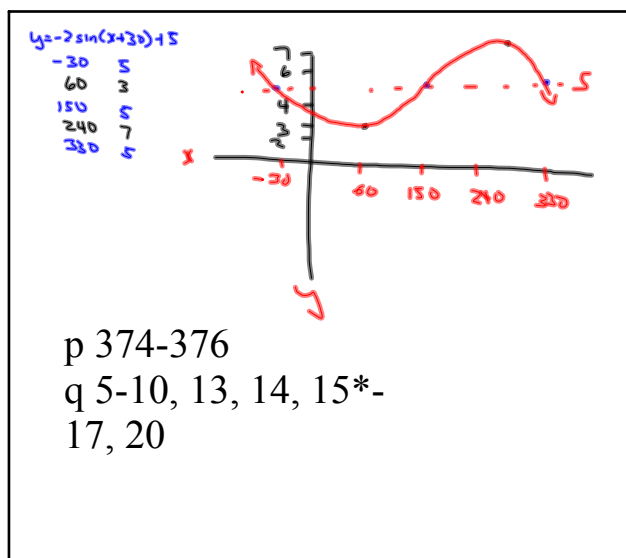
$$y = \sin(x)$$

$$y = -2 \sin(x+30) + 5$$

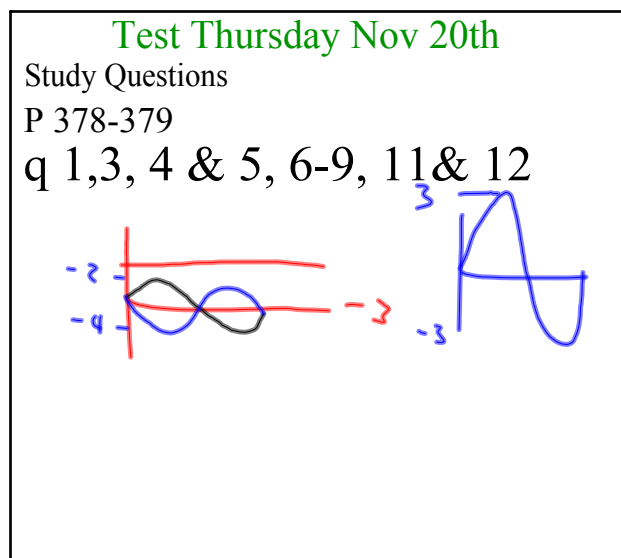
0	0
90	+1
180	0
270	-1
360	0

-30	5
60	3
150	5
240	7
330	5

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May 5-2:20 PM



May 5-2:28 PM